



Laser Ranging for Sustainable Millimeter Geoscience

Tab 1. Characteristics of PMF solution

Ray-tracing software

Ray tracing method

Data source (NWM)

**Elevation granularity** Horizontal resolution

NWM horizontal resolution NWM vertical resolution

Parameter





POTSDAM

description

GFZ direct numerical simulation (DNS) tool

Extended troposphere delay model dedicated to Satellite Laser Ranging

SERC

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Motivation

Satellite Laser Ranging (SLR) is the only space geodetic technique in which troposphere models do not consider horizontal asymmetry of the atmosphere above the station. Due to low number of observations, poor geometry, and weather conditions the estimation of horizontal gradients from laser observation provide to deterioration of weekly solutions. To model this effect in sufficient way we propose to use the ray-traced mapping function coefficients and the horizontal gradients dedicated for laser observations.

Monument Peak

## Methodology

2D

ERA-Interim 0.5° x 0.5°

3,5,7,10,15,20,30,50,70,90

60 levels

30 degrees

PMF products	
1.3 ×10 <sup>-3</sup> al	1.32 ×10 <sup>-3</sup> al
1.28 Mendes- PMF	Pavlis 1.3
1.26	128 128 12
1.24	
1.22	
1.2	1.24
1.18 i i i i i i i i i i i i i i i i i i i	1.22 at ×10 <sup>-3</sup> a2
a.t	3.05
3 m will the play the have	True 3
2.9	2.05
and the part is	2.9 Very Arres of the Warrington
1.	2.85
2.7 a3	2.8 83
1.068	
0.066	0.065
0.064	0.064
0.062	0.063
0.06 I	0.062
0.058 Jap07 Apr07 Jpl07 Oct07	0.061 0.061

rig. 1. Comparison of mapping function coefficients, a1, a2, a3 derived from FCULa and from PMF mapping functions. For year 2007. For station GRAZ (left) and Yarragadee (7090).

The time series of mapping function coefficients derived from Mendes - Pavlis model (red) and NWM solution (Green) are shown in figure 1. The a1 coefficient derived from NWM is smoothed in comparison to a1 MP coefficient. Moreover, the coefficients a2 and a3 show characteristic offset at the level of 3% to 6%. The impact of the differences between coefficients from PMF and Mendes-Pavlis models is transformed to differences of the slant total delay estimation at the level of 5 mm for the elevation angle equal to 10 degrees (fig 2).



## $\begin{bmatrix} -- & - & 10^\circ & PMF \\ - & - & 10^\circ & PMF + & O1 \\ 0 & & 10^\circ & PMF + & O1 + & O2 \end{bmatrix}$ azimuth

Gras

Fig 3. Impact of the first (green dashed line) and second degree (red doted line) of PMF Horizontal gradients for 10° elevation angle, at the 28 January 2007. The second degree of horizontal agradients improves the horizontal asymetricity above SLR station. The differences between linear gradients can reach even 11





Horizontal gradients and mapping function coefficients are derived using ray-trace algorithm developed by Zus et al., (2014). The state vector of PMF consists of the mapping function coefficients  $a_1$ ,  $a_2$ ,  $a_3$  and the horizontal gradients of the first ( $G_{N'}$  $G_{E}$ ) and the second order ( $G_{NN'}$   $G_{NE'}$  and  $G_{EE}$ ). PMF is estimated for all SLR stations with time resolution equal to 6 hours. For each station, 120 slants factors as well as mapping factors were computed (Table 1). In the second step the zenith delays are applied to obtain the azimuth-dependent and azimuth independent slant delays. Finally, the mapping function coefficients and  $G_{N'}$ ,  $G_{E'}$ ,  $G_{NN'}$ ,  $G_{NE'}$  and  $G_{EE}$  are estimated using the least-square fitting. We present three solutions: PMF - which is based only on the new mapping function coefficients, PMF+O1 - including the new mapping function coefficient and linear horizontal gradients, and PMF + O1 + O2 which considers the PMF mapping function coefficients and linear and non linear horizontal gradients. The solutions mentioned above are compared with the standard Mendes - Pavlis (MP) model using observations to Lageos 1 and Lageos 2.



We can observe the improvements of interquartile distance of the SLR observation residuals to Lageos - 1/2 solutions with horizontal gradients at the level of 1.1, 1.5 and 1.7 for stations Graz, Yarragadee and Grasse

based on PMF mapping functions and horizontal gradients. The largest improvement due to using PMF model is for station

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## Geocenter coordinates

The negative values correspond to the improvement for solutions





Figure 7 presents the differences between pole coordinates including PMFs models and Mendes-Pavlis approach. The solutions with horizontal gradients characterize offsets at the level of 20 µas. The consistency of the pole coordinates between SLR solutions with horizontal gradients and the IERS-14-C04 series is improved and reduced from 22 µas and 38 µas to 2 µas and 14 µas for X and Y pole coordinates, respectively.

The differences of the geocenter coordinates are shown in figure 8. The mean shift in the solution PMF+O1 and O2 is up to 0.04, -0.13, -0.04 mm for the X, Y, and Z components which suggests that the currently used origin of the ITRF realization may be affected by neglection of horizontal gradients in the SLR solutions.



## Conclusions

We propose to extend the currently used troposphere delay model by linear horizontal gradients derived from NWM. The mapping functions coefficients give the same results as the mapping function coefficient derived from FCULzd proposed by Mendes and Pavlis 2002. The horizontal gradients improve the consistency between SLR and other space geodetic techniques. The nonlinear horizontal gradients bring measurable results in dynamic weather conditions however the SLR stations provide observations only in good cloudless conditions so the second degree of horizontal gradients could be neglected to simplify the troposphere model

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